

AP Calculus Integration Practice

AP Calculus Integration Practice - 53 questions

53 Questions | 106 min

1. Evaluate the integral: $\int x^3 \sqrt{4 + x^4} dx$

2. Evaluate the integral: $\int \frac{dx}{x \ln x}$

3. Evaluate the integral: $\int \frac{(x + 5)dx}{\sqrt{x + 4}}$

4. Find the integer n that allows for integration by substitution, then evaluate: $\int x^n \sqrt{1-x^4} dx$

5. Find the integer n that allows for integration by substitution (two natural choices exist), then evaluate: $\int \frac{x^n}{\sqrt{1-x^4}} dx$

6. Find the integer n that allows for integration by substitution (two natural choices exist), then evaluate: $\int \frac{x^n}{1+x^{10}} dx$

7. Find the integer n that allows for integration by substitution, then evaluate: $\int \frac{x^6}{1+x^n} dx$

8. Find the integer n that allows for integration by substitution, then evaluate: $\int x^n e^{-x^2} dx$

9. Find the integer n that allows for integration by substitution, then evaluate: $\int x^n e^{2x^5} dx$

10. Find the integer n that allows for integration by substitution, then evaluate: $\int x^5 \sqrt{1 - x^n} dx$

11. Find the integer n that allows for integration by substitution, then evaluate: $\int \frac{x^6}{\sqrt{1 - x^n}} dx$

12. Find the integer n that allows for integration by substitution, then evaluate: $\int \frac{dx}{x^n \ln x}$

13. Find the integer n that allows for integration by substitution, then evaluate: $\int \frac{dx}{x^n (\ln x)^7}$

14. Find the integer n that allows for integration by substitution, then evaluate: $\int x^n \sin(x^6) dx$

15. Find the integer n that allows for integration by substitution, then evaluate: $\int \frac{\sin^n x \cos x}{\sqrt{3 + \sin^4 x}} dx$

16. Find the integer n that allows for integration by substitution, then evaluate: $\int \frac{\sin^3 x \cos x}{\sqrt{3 + \sin^n x}} dx$

17. Evaluate the integral: $\int x e^{-\frac{x}{10}} dx$

18. Evaluate the integral: $\int x^2 e^{-\frac{x}{10}} dx$

19. Evaluate the integral: $\int x^2 \ln x dx$

20. Evaluate the integral for integer $n \neq -1$: $\int x^n \ln x dx$

21. Evaluate the integral: $\int x^2 \sin x dx$

22. Evaluate the integral: $\int x^3 e^{-x^2} dx$

23. Evaluate the integral: $\int x^3 \sqrt{x^2 + 1} dx$

24. Given that $\int f(x) dx = g(x)$ and $\int g(x) dx = h(x)$, compute: $\int x^3 f(x^2) dx$

25. Given that $\int f(x)dx = g(x)$ and $\int g(x)dx = h(x)$, compute: $\int x^{2n-1}f(x^n)dx$

26. Evaluate the integral: $\int \sin^{-1} x dx$

27. Evaluate the integral: $\int (\sin^{-1} x)^2 dx$

28. Evaluate the integral: $\int \tan^{-1} x dx$

29. Evaluate the integral: $\int \sec^3 \theta d\theta$

Hint: Write $\sec^3 \theta = \sec \theta(1 + \tan^2 \theta)$ and integrate $\sec \theta \tan^2 \theta$ by parts.

30. Evaluate the integral: $\int \frac{\sqrt{9 - x^2}}{x^2} dx$

31. Evaluate the integral: $\int \frac{dx}{x\sqrt{1-x^2}}$

32. Evaluate the integral: $\int \frac{dx}{x\sqrt{a^2+x^2}}$

33. Evaluate the integral: $\int \sqrt{4+x^2} dx$

Hint: See Problem 12 on page 3 (integral of $\sec^3 \theta$).

34. Evaluate the integral: $\int \frac{dx}{a^2 - x^2}$

Note: It might be easier to do this by partial fractions.

35. Evaluate the integral: $\int \frac{\sqrt{x^2 - a^2}}{x} dx$

36. Evaluate the integral: $\int \frac{dx}{(a^2 + x^2)^2}$

37. Evaluate the integral using the substitution $x = \sin \theta$: $\int \sin^{-1} x dx$

38. Evaluate the integral: $\int (\sin^{-1} x)^2 dx$

39. Evaluate the integral: $\int \tan^{-1} x dx$

40. Evaluate the integral: $\int \frac{5x - 3}{x^2 - 2x - 3} dx$

41. Evaluate the integral: $\int \frac{6x + 7}{(x + 2)^2} dx$

42. Evaluate the integral: $\int \frac{2x^3 - 4x^2 - x - 3}{x^2 - 2x - 3} dx$

43. Evaluate the integral: $\int \frac{dx}{x(x^2 + 1)}$

44. Evaluate the integral: $\int \left(\frac{1}{x^2 + 1} - \frac{1}{x^2 - 2x + 5} \right) dx$

45. Evaluate the integral: $\int \frac{x^3 + 2x^2 + 2}{(x^2 + 1)^2} dx$

46. Evaluate the definite integral: $\int_0^{\frac{\pi}{2}} \frac{3}{1 + \sin \theta} d\theta$

47. Evaluate the definite integral: $\int_0^{2\frac{\pi}{3}} \frac{3}{5 + 4 \cos \theta} d\theta$

48. Evaluate the definite integral: $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{3}{4 + 5 \cos \theta} d\theta$

49. Evaluate the definite integral: $\int_0^{\frac{\pi}{2}} \frac{5}{3 \sin \theta + 4 \cos \theta} d\theta$

50. Solve the initial value problem: $\frac{dy}{dx} = xy, y(0) = 1$

51. Solve the initial value problem: $y \frac{dy}{dx} = x^2, y(0) = 1$

52. Solve the initial value problem: $\frac{dy}{dx} = -2x(y + 3), y(0) = 1$

53. Solve the initial value problem: $\frac{dy}{dx} = \frac{x^2y + y}{x^2 - 1}, y(0) = 2$